

## FORMS OF ANSWERS

The following list explains acceptable forms for answers. Coaches should ensure that Mathletes are familiar with these rules prior to participating at any level of competition. Judges will score competition answers in compliance with these rules for forms of answers.

**All answers must be expressed in simplest form.** A “common fraction” is to be considered a fraction in the form  $\pm \frac{a}{b}$ , where  $a$  and  $b$  are natural numbers and  $\text{GCF}(a, b) = 1$ . In some cases the term “common fraction” is to be considered a fraction in the form  $\frac{A}{B}$ , where  $A$  and  $B$  are algebraic expressions and  $A$  and  $B$  do not share a common factor. A simplified “mixed number” (“mixed numeral,” “mixed fraction”) is to be considered a fraction in the form  $\pm N \frac{a}{b}$ , where  $N$ ,  $a$  and  $b$  are natural numbers,  $a < b$  and  $\text{GCF}(a, b) = 1$ . Examples:

*Problem:* Express 8 divided by 12 as a common fraction.      *Answer:*  $\frac{2}{3}$       *Unacceptable:*  $\frac{4}{6}$   
*Problem:* Express 12 divided by 8 as a common fraction.      *Answer:*  $\frac{3}{2}$       *Unacceptable:*  $\frac{12}{8}, 1\frac{1}{2}$   
*Problem:* Express the sum of the lengths of the radius and the circumference of a circle with a diameter of  $\frac{1}{4}$  as a common fraction in terms of  $\pi$ .      *Answer:*  $\frac{1+2\pi}{8}$   
*Problem:* Express 20 divided by 12 as a mixed number.      *Answer:*  $1\frac{2}{3}$       *Unacceptable:*  $1\frac{8}{12}, \frac{5}{3}$

**Ratios should be expressed as simplified common fractions** unless otherwise specified. Examples:

*Simplified, Acceptable Forms:*  $\frac{7}{2}, \frac{3}{\pi}, \frac{4-\pi}{6}$       *Unacceptable:*  $3\frac{1}{2}, \frac{1}{3}, 3.5, 2:1$

**Radicals must be simplified.** A simplified radical must satisfy: 1) no radicands have a factor which possesses the root indicated by the index; 2) no radicands contain fractions; and 3) no radicals appear in the denominator of a fraction. Numbers with fractional exponents are *not* in radical form. Examples:

*Problem:* Evaluate  $\sqrt{15} \times \sqrt{5}$ .      *Answer:*  $5\sqrt{3}$       *Unacceptable:*  $\sqrt{75}$

**Answers to problems asking for a response in the form of a dollar amount or an unspecified monetary unit (e.g., “How many dollars...,” “How much will it cost...,” “What is the amount of interest...”) should be expressed in the form (\$)  $a.bc$ , where  $a$  is an integer and  $b$  and  $c$  are digits.**

The *only* exceptions to this rule are when  $a$  is zero, in which case it may be omitted, or when  $b$  and  $c$  are both zero, in which case they may both be omitted. Examples:

*Acceptable:* 2.35, 0.38, .38, 5.00, 5      *Unacceptable:* 4.9, 8.0

**Units of measurement are not required in answers, but they must be correct if given.** When a problem asks for an answer expressed in a specific unit of measure or when a unit of measure is provided in the answer blank, equivalent answers expressed in other units are not acceptable. For example, if a problem asks for the number of ounces and 36 oz is the correct answer, 2 lbs 4 oz will not be accepted. If a problem asks for the number of cents and 25 cents is the correct answer, \$0.25 will not be accepted.

**Do not make approximations for numbers** (e.g.,  $\pi$ ,  $\frac{2}{3}$ ,  $5\sqrt{3}$ ) in the data given or in solutions unless the problem says to do so.

**Do not do any intermediate rounding** (other than the “rounding” a calculator performs) when calculating solutions. All rounding should be done at the end of the calculation process.

**Scientific notation** should be expressed in the form  $a \times 10^n$  where  $a$  is a decimal,  $1 \leq |a| < 10$ , and  $n$  is an integer. Examples:

*Problem:* Write 6895 in scientific notation.      *Answer:*  $6.895 \times 10^3$   
*Problem:* Write 40,000 in scientific notation.      *Answer:*  $4 \times 10^4$  or  $4.0 \times 10^4$

**An answer expressed to a greater or lesser degree of accuracy than called for in the problem will not be accepted. Whole number answers should be expressed in their whole number form.**

Thus, 25.0 will not be accepted for 25 nor vice versa.

**The plural form of the units will always be provided in the answer blank, even if the answer appears to require the singular form of the units.**

## VOCABULARY AND FORMULAS

The following list is representative of terminology used in the problems but should not be viewed as all-inclusive. It is recommended that coaches review this list with their Mathletes.

abscissa	degree measure	interior angle of a polygon
absolute value	denominator	intersection
acute angle	diagonal of a polygon	inverse variation
additive inverse (opposite)	diagonal of a polyhedron	irrational number
adjacent angles	diameter	isosceles
algorithm	difference	lateral surface area
alternate interior angles	digit	lateral edge
alternate exterior angles	digit-sum	lattice point(s)
altitude (height)	direct variation	LCM
area	dividend	linear equation
arithmetic mean	divisible	mean
arithmetic sequence	divisor	median of a set of data
base 10	edge	median of a triangle
binary	endpoint	midpoint
bisect	equation	mixed number
box-and-whisker plot	equiangular	mode(s) of a set of data
center	equidistant	multiple
chord	equilateral	multiplicative inverse (reciprocal)
circle	evaluate	natural number
circumference	expected value	numerator
circumscribe	exponent	obtuse angle
coefficient	expression	octagon
collinear	exterior angle of a polygon	octahedron
combination	factor	odds (probability)
common denominator	factorial	opposite of a number (additive inverse)
common divisor	Fibonacci sequence	ordered pair
common factor	finite	ordinate
common fraction	formula	origin
common multiple	frequency distribution	palindrome
complementary angles	frustum	parallel
composite number	function	parallelogram
compound interest	GCF	Pascal's triangle
concentric	geometric mean	pentagon
cone	geometric sequence	percent increase/decrease
congruent	height (altitude)	perimeter
convex	hemisphere	permutation
coordinate plane/system	hexagon	perpendicular
coordinates of a point	hypotenuse	planar
corresponding angles	image of a point (under a transformation)	polygon
counting numbers	improper fraction	polyhedron
counting principle	inequality	prime factorization
cube	infinite series	prime number
cylinder	inscribe	principal square root
data	integer	
decimal		

prism	remainder	system of equations/ inequalities
probability	repeating decimal	tangent figures
product	revolution	tangent line
proper divisor	rhombus	term
proper factor	right angle	terminating decimal
proper fraction	right circular cone	tetrahedron
proportion	right circular cylinder	total surface area
pyramid	right polyhedron	transformation
Pythagorean Triple	right triangle	translation
quadrant	rotation	trapezoid
quadrilateral	scalene triangle	triangle
quotient	scientific notation	triangular numbers
radius	segment of a line	trisect
random	semicircle	union
range of a data set	sequence	unit fraction
rate	set	variable
ratio	similar figures	vertex
rational number	simple interest	vertical angles
ray	slope	volume
real number	slope-intercept form	whole number
reciprocal (multiplicative inverse)	solution set	$x$ -axis
rectangle	sphere	$x$ -coordinate
reflection	square	$x$ -intercept
regular polygon	square root	$y$ -axis
relatively prime	stem-and-leaf plot	$y$ -coordinate
	sum	$y$ -intercept
	supplementary angles	

The list of formulas below is representative of those needed to solve MATHCOUNTS problems but should not be viewed as the only formulas that may be used. Many other formulas that are useful in problem solving should be discovered and derived by Mathletes.

#### CIRCUMFERENCE

Circle  $C = 2 \times \pi \times r = \pi \times d$

#### AREA

Square  $A = s^2$

Rectangle  $A = l \times w = b \times h$

Parallelogram  $A = b \times h$

Trapezoid  $A = \frac{1}{2}(b_1 + b_2) \times h$

Circle  $A = \pi \times r^2$

Triangle  $A = \frac{1}{2} \times b \times h$

Triangle  $A = \sqrt{s(s-a)(s-b)(s-c)}$

Equilateral triangle  $A = \frac{s^2 \sqrt{3}}{4}$

Rhombus  $A = \frac{1}{2} \times d_1 \times d_2$

#### SURFACE AREA & VOLUME

Sphere  $SA = 4 \times \pi \times r^2$

Sphere  $V = \frac{4}{3} \times \pi \times r^3$

Rectangular prism  $V = l \times w \times h$

Circular cylinder  $V = \pi \times r^2 \times h$

Circular cone  $V = \frac{1}{3} \times \pi \times r^2 \times h$

Pyramid  $V = \frac{1}{3} \times B \times h$

Pythagorean Theorem  $c^2 = a^2 + b^2$

Counting/  
Combinations  ${}_n C_r = \frac{n!}{(r!)(n-r)!}$